

Q.1. Mean = Median = Mode = Range

↓  
4, 10, 10, 12, 14

↓  
satisfied

mode = 10

median = 10

range = 14 - 4 = 10

mean = 10

base  $\times 2$   $\left( \begin{array}{c} \text{2nd no} \\ \text{3rd no} \end{array} \right) \boxed{25567}$

we can find infinite sets of numbers from the base no.:

One way  $\boxed{410101214}$

↓  
infinite

another base  $\left( \begin{array}{c} \text{3rd} \\ \text{4th} \end{array} \right) \boxed{34558}$

we again can find

6 8 10 10 | mode = 5

infinite sets

all 10 | median = 5

range = 5

infinite mean = 5

- one more set 8 20 20 24 28  
from 4 10 10 12 14

till infinite

Why this doubling trick works.  
Have to prove this

For mode

this is our example

2	5	5	6	7
4	10	10	12	14

suppose 2 5 5 6 7

4	10	10	12	14
2x	2y	2y		

mode = 5  $\rightarrow 5 \times 2 = 10$

median = 5

range = 5

mean = 5

naturally

the y is repeated so  
2y is also repeated

It is convinced that if everything is  
doubled, mode is also doubled

For median

position wise

2 5 5 6 7

4 10 10 12 14

it will be doubled as well

For range

so first in 2 5 5 6 7

range is ~~7-5~~

7-2 originally

new range =  $(7 \times 2) - (2 \times 2)$

=  $2(7-2)$

For mean

For that this part is common

$$2 \left[ \frac{\quad}{5} \right]$$

when you are doubling the whole set then that doubles the whole sum of it and then ~~just~~ you can divide it by 5

that's why this is common  $2 \left( \frac{\quad}{5} \right)$   
original  $\rightarrow \frac{\quad}{5}$

new mean #

in 4 10 10 12 14

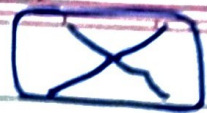
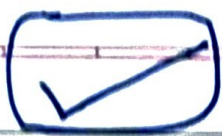
$$= \frac{(4 + 10 + 10 + 12 + 14)}{5}$$

in short =  $2 \left( \frac{2 + 5 + 5 + 6 + 7}{5} \right)$

new mean is  $\times 2$  the mean of original original mean set

For base set you need some trial and error:

: By changing the multiplier, we can find infinite sets.



Q.2. a) Mode < Median < Mean

= 5, 5, 6, 7, 12

mode - 5

median - 6

mean -  $\frac{35}{5} = 7$

can't repeat  
8, 8, 8, 10, 11  
mode - 8  
median - also 8  
so its wrong

2 B) Mode < Mean < ~~Mean~~ Median

= 1, 1, 10, 11, 12

mode - 1

median - 7

mean - 10

experimenting  $\times 2$  1, 1, 10, 11, 12 let's see if  
2, 2, 20, 22, 24 it works in  
this case

mode - 2

median - ~~7~~ 14

mean - 20

now again  
you can generate  
infinite sets with  
this condition.

again like

3, 3, 30, 33, 36

2 c) Mean < Mode < Median

= 2 16 20 20 22

1 8 10 10 11

won't work

so

just trial and error

5 5 6 \_\_\_\_\_

mode < ~~median~~ median

fixed place for mode it must come there

Take example of 5, 5 <sup>+1</sup> 6

~~we need answer in~~ whole numbers

the no's are

Sum = 4

5

total has to be 20 or smaller.

To reach 20 you already have

$$5 + 5 + 6 = 16$$

3 <sup>4</sup> 1

won't work

So it is not possible

2 D) Mean < Median < Mode

= 1, 2, 5, 6, 6

mode - 6

median - 5

mean - 4

1 2 4 5 5

mode - 5

median - 4 } smaller anyway

mean - 3. something

In decimals

2 E) Median < Mode < Mean

\_\_\_\_\_ 10    11    11    30    30  
                   ↑                    ~ mode

+ = 70

mean bigger than 30 not possible

Not possible

~~be~~ because it has to be in ascending order

2 F) Median < Mean < mode

= 4 5 6 10 10

possible

median - 6 }  
mean - 7 }  
mode - 10 }

again you can ~~be~~ find infinite examples by doubling it further.