

CHARLIE (Keep It Simple PT I)

Does the left hand side = Right hand side?

$\frac{1}{2} = \frac{1}{10} + \frac{1}{20}$  ✓  
 $\frac{1}{3} = \frac{1}{4} + \frac{1}{12}$  ✓  
 $\frac{1}{3} = \frac{1}{7} + \frac{1}{21}$  ✗  
 $\frac{1}{4} = \frac{1}{5} + \frac{1}{20}$  ✓

To prove:  
 $\frac{1}{n} = \frac{1}{n+1} + \frac{1}{n(n+1)}$  (Working on Right hand side)  
 $\frac{n+1}{n(n+1)} = \frac{1 \times (n+1)}{n \times (n+1)}$   
 $= \frac{1}{n}$  PROVEN

P.S This rule doesn't cover all possibilities. But it will always work. And Charlie will find a lot of correct answers if he uses this equation.

ALYSON (Keep It Simple PT II)

Same as

$\frac{1}{6} = \frac{1}{7} + \frac{1}{42}$  ✗  
 $\frac{1}{6} = \frac{1}{8} + \frac{1}{24}$  ✓  
 $\frac{1}{6} = \frac{1}{9} + \frac{1}{18}$  ✗  
 $\frac{1}{6} = \frac{1}{10} + \frac{1}{15}$  ✓  
 $\frac{1}{6} = \frac{1}{12} + \frac{1}{12}$  (This doesn't count.)

Yes, all unit fractions can be made like this and using this method.

UNIT FRACTIONS

$\frac{1}{6}$	$\frac{1}{7}$	$\frac{1}{8}$	$\frac{1}{9}$	$\frac{1}{10}$	$\frac{1}{11}$	$\frac{1}{12}$
$\frac{1}{6} = \frac{1}{7} + \frac{1}{42}$	$\frac{1}{6} = \frac{1}{8} + \frac{1}{24}$	$\frac{1}{6} = \frac{1}{9} + \frac{1}{18}$	$\frac{1}{6} = \frac{1}{10} + \frac{1}{15}$	$\frac{1}{6} = \frac{1}{11} + \frac{1}{66}$	$\frac{1}{6} = \frac{1}{12} + \frac{1}{12}$	$\frac{1}{6} = \frac{1}{12} + \frac{1}{12}$
$\frac{1}{7} = \frac{1}{8} + \frac{1}{56}$	$\frac{1}{7} = \frac{1}{9} + \frac{1}{63}$	$\frac{1}{7} = \frac{1}{10} + \frac{1}{70}$	$\frac{1}{7} = \frac{1}{11} + \frac{1}{77}$	$\frac{1}{7} = \frac{1}{12} + \frac{1}{84}$	$\frac{1}{7} = \frac{1}{13} + \frac{1}{91}$	$\frac{1}{7} = \frac{1}{14} + \frac{1}{49}$
$\frac{1}{8} = \frac{1}{9} + \frac{1}{72}$	$\frac{1}{8} = \frac{1}{10} + \frac{1}{80}$	$\frac{1}{8} = \frac{1}{11} + \frac{1}{88}$	$\frac{1}{8} = \frac{1}{12} + \frac{1}{96}$	$\frac{1}{8} = \frac{1}{13} + \frac{1}{104}$	$\frac{1}{8} = \frac{1}{14} + \frac{1}{112}$	$\frac{1}{8} = \frac{1}{15} + \frac{1}{120}$
$\frac{1}{9} = \frac{1}{10} + \frac{1}{90}$	$\frac{1}{9} = \frac{1}{11} + \frac{1}{99}$	$\frac{1}{9} = \frac{1}{12} + \frac{1}{108}$	$\frac{1}{9} = \frac{1}{13} + \frac{1}{117}$	$\frac{1}{9} = \frac{1}{14} + \frac{1}{126}$	$\frac{1}{9} = \frac{1}{15} + \frac{1}{135}$	$\frac{1}{9} = \frac{1}{16} + \frac{1}{144}$
$\frac{1}{10} = \frac{1}{11} + \frac{1}{110}$	$\frac{1}{10} = \frac{1}{12} + \frac{1}{120}$	$\frac{1}{10} = \frac{1}{13} + \frac{1}{130}$	$\frac{1}{10} = \frac{1}{14} + \frac{1}{140}$	$\frac{1}{10} = \frac{1}{15} + \frac{1}{150}$	$\frac{1}{10} = \frac{1}{16} + \frac{1}{160}$	$\frac{1}{10} = \frac{1}{17} + \frac{1}{170}$
$\frac{1}{11} = \frac{1}{12} + \frac{1}{132}$	$\frac{1}{11} = \frac{1}{13} + \frac{1}{143}$	$\frac{1}{11} = \frac{1}{14} + \frac{1}{154}$	$\frac{1}{11} = \frac{1}{15} + \frac{1}{165}$	$\frac{1}{11} = \frac{1}{16} + \frac{1}{176}$	$\frac{1}{11} = \frac{1}{17} + \frac{1}{187}$	$\frac{1}{11} = \frac{1}{18} + \frac{1}{198}$
$\frac{1}{12} = \frac{1}{13} + \frac{1}{156}$	$\frac{1}{12} = \frac{1}{14} + \frac{1}{168}$	$\frac{1}{12} = \frac{1}{15} + \frac{1}{180}$	$\frac{1}{12} = \frac{1}{16} + \frac{1}{192}$	$\frac{1}{12} = \frac{1}{17} + \frac{1}{204}$	$\frac{1}{12} = \frac{1}{18} + \frac{1}{216}$	$\frac{1}{12} = \frac{1}{19} + \frac{1}{228}$

Charlie's Calculations

Algebraic Statements  
 $\frac{1}{n} = \frac{1}{m} + \frac{1}{n \times m}$  where both  $n$  and  $m$  are integers,  $n < m$  and  $n > 0$