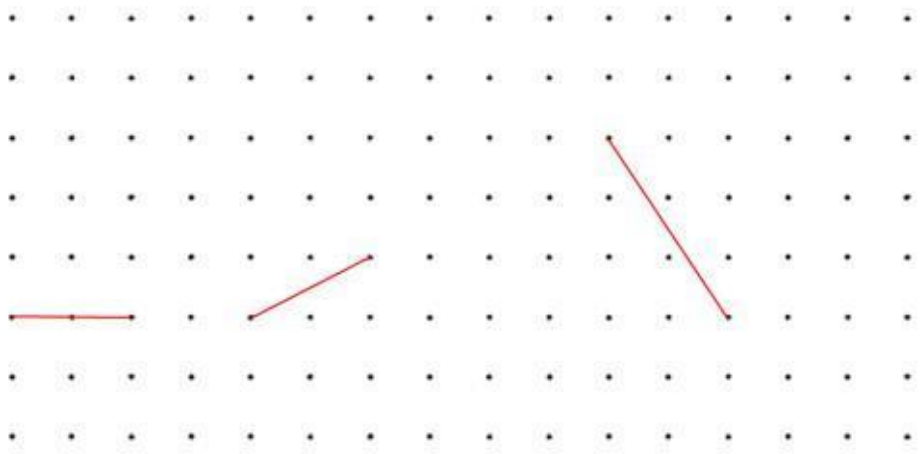
Opposite Vertices - Squares

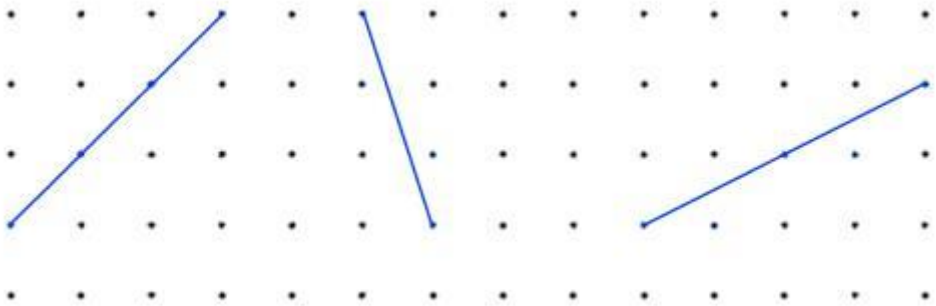
Charlie has been exploring squares with vertices drawn on the points of a square dotty grid. Unfortunately he rubbed out some of his work and only left behind one side of each square.



Can you recreate the squares he drew?
Is there more than one possibility?

Could **any** line joining two points be the side of a square whose vertices lie on grid points? How can you be sure?

Alison has been drawing squares and their diagonals. Here are some of the diagonals she drew:



Can you recreate the squares she drew from her diagonals?
Is there more than one possibility?

Can you find a method to draw a square when you are just given the diagonal?

Could **any** line joining two points be the diagonal of a square whose vertices lie on grid points?

Can you find a way to help Alison decide whether a given line could be the diagonal of such a square?