



Stage 4 ★
Mixed Selection 2 – Solutions

1. In the hundreds

If $\frac{1}{2}n$ is a three-digit whole number, then n is an even number between 200 and 1998 inclusive.

Since we also want $2n$ to be a three-digit whole number, n must be an even number between 200 and 499 inclusive.

There are 150 such numbers.

2. Weighing the baby

Let m be my weight, b be the baby's weight and n be the nurse's weight.

We have:

$$m + b = 78$$

$$b + n = 69$$

$$m + n = 137$$

Adding all three equations together we get

$$(m + b) + (b + n) + (m + n) = 78 + 69 + 137 \Rightarrow 2(b + m + n) = 284 \\ \Rightarrow b + m + n = 142. \text{ So the combined weight is 142kg.}$$

3. Near 10

We require that $-1 < \sqrt{n} - 10 < 1 \Rightarrow 9 < \sqrt{n} < 11 \Rightarrow 81 < n < 121$.

Hence the possible integer values for n are the 39 values

$$n = 82, 83, \dots, 119, 120.$$

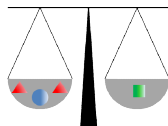
These problems are adapted from UKMT Mathematical Challenge problems (ukmt.org.uk).



4. Weighing scales

Say a cone weighs x , a sphere weighs y and a cube weighs z .

Then (1) $2x + y = z$ since two cones and a sphere together weigh the same as a cube.



Also, (2) $y + z = 3x$ since a sphere and a cube together weigh the same as three cones.



Taking y from each side of (1) (or taking a sphere from each side of the first scales) gives (3) $2x = z - y$

Then to find out how much one cone weighs, we take equation (3) from equation (2) to give

$$3x - 2x = (y + z) - (z - y)$$

$$\Rightarrow x = y + z - z + y$$

$$\Rightarrow x = 2y$$

So a cone weighs the same as two spheres.

5. I love musical stars

Consider the third column:

$$2\text{♩} + \text{♥} = 13 \quad (1)$$

and the second row:

$$\text{♩} + 2\text{♥} = 11 \quad (2)$$

$2 \times (2) - (1)$ yields:

$$3\text{♥} = 9$$

$$\text{So } \text{♥} = 3.$$

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