

Exploring Quadratic Mappings

These are my conclusions

A quadratic function is usually written in the form of $f(x) = ax^2 + bx + c$

I applied various values to x and a,b,c remained constant. Then I put the results on an x,y table and then plotted them on a graph.

A) I found that as a quadratic graph always has x^2 it will be a **curved** graph and will have a parabola. The parabola will open upwards if a is more than 0 and will open downwards when the value of a is less than 0.

Each parabola is **symmetrical** because it is ax^2 —when numbers are squared as below you get a symmetrical pattern and when they are plotted on a graph you get a parabola.

X	-4	-3	-2	-1	0	1	2	3	4
Y	16	9	4	1	0	1	4	9	16

You can also find the exact **axis of symmetry** by $x = -b/2a$. This will give you the x coordinate of the axis of symmetry.

B) From a quadratic mapping you can tell a graph will **cross** the x axis always when $y = 0$

And you can tell the graph will cross the y axis when x is 0 or c. But a quadratic function can have one, two or no x intercepts.

C) The **vertex** is the lowest point or the highest point of the graph depending upon whether the parabola is upwards or downwards. If x^2 is positive then the vertex is the lowest point and if x^2 is negative then it is the highest point of the graph. You can tell the points of the vertex from the mapping as they are the lowest part- eg

For the $f(x) = 2x^2 - 4x + 5$

X	-2	-1	0	1	2
F(x)	21	11	5	3	5

Here the vertex coordinates are 1,3.

You can also tell the points of a vertex if you know the axis of symmetry.

So for a function $f(x) = 2x^2 - 4x + 5$ the axis of symmetry is $x = -b/2a$ and here it is $4/2 \times 2 = 1$ which is the "x" coordinate.

The "y" coordinate is $f(x^2) = +bx + c = y$. So here it is $2(1^2) - 4(1) + 5 = 3$

So the lowest point of the vertex are the coordinates (1,3)