The converse of Pythagoras' theorem states that:
"If a triangle has lengths $a, b$ and $c$ which satisfy $a^{2}+b^{2}=c^{2}$ then it is a right-angled triangle."

Here is a diagram, and a proof that if $a^{2}+b^{2}=c^{2}$ then $C$ cannot be less than $90^{\circ}$, but the proof has been scrambled up.
Can you rearrange it into its original order?


| Expanding gives $x^{2}+y^{2}+b^{2}=b^{2}-2 b x+x^{2}+y^{2}$ | A |
| :--- | :--- |
| Let $C X=x$ and so we have $A X=b-x$, and also let $B X=y$ | B |
| If $x=0$ then point $X$ is at the same place as point $C$, which means that $\angle A C B=90^{\circ}$ | C |
| This means that either $b=0$, which is not possible as $b$ is the length of a side of <br> the triangle, or $x=0$ | D |
| $\triangle C X B$ is right-angled, so we have $x^{2}+y^{2}=a^{2}$ | E |
| If $C<90^{\circ}$ then there will be a point $X$ on side $A C$ such that $\angle A X B=90^{\circ}$ | F |
| This contradicts our initial statement that angle $C$ is less than $90^{\circ}$, and so $C$ cannot <br> be less than $90^{\circ}$ | G |
| We start by assuming that there exists a triangle $A B C$ with lengths $a, b$ and $c$ where <br> $a^{2}+b^{2}=c^{2}$, and angle $C$ is less than $90^{\circ}$ | H |
| We have $a^{2}+b^{2}=c^{2}$ and substituting for $a^{2}$ and $c^{2}$ gives <br> $\left(x^{2}+y^{2}\right)+b^{2}=(b-x)^{2}+y^{2}$ | I |
| $\triangle A X B$ is right-angled, so we have $(b-x)^{2}+y^{2}=c^{2}$ | J |
| Simplifying gives $2 b x=0$ |  |

