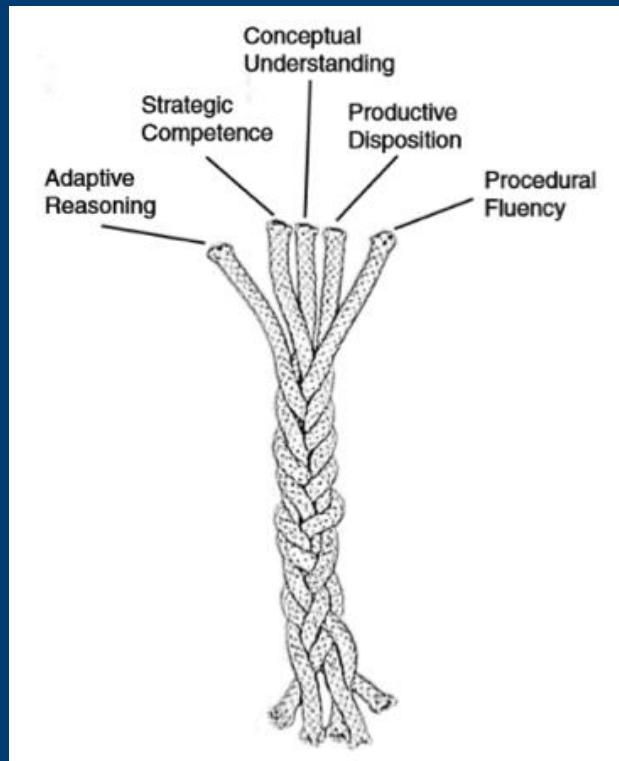


# **Purposeful practice: Consolidating understanding using rich tasks**

Alison Kiddle



# Strands of Mathematical Proficiency



Kilpatrick, J. Swafford, J. & Findell, B.(eds.)(2001). Adding it up: Helping children learn mathematics. Mathematics Learning Study Committee: National Research Council.



# Consolidating with rich tasks

To:

Deepen understanding

Build connections

Develop fluency



# Isosceles Triangles

Draw some isosceles triangles with an area of  $9 \text{ cm}^2$  and a vertex at  $(20, 20)$ .

If all the vertices have whole number coordinates, how many is it possible to draw?

Can you explain how you know that you have found them all?



# Unequal Averages

Here's an interesting set of five numbers:

2,5,5,6,7

Mean, mode, median and range are all 5.

**Can you find other sets of five positive whole numbers where:**

**Mean = Median = Mode = Range**



# Unequal Averages

Can you find sets of five positive whole numbers that satisfy the following properties?

Mode < Median < Mean

Mean < Median < Mode

Mode < Mean < Median

Median < Mode < Mean

Mean < Mode < Median

Median < Mean < Mode



There are many more NRICH tasks that offer opportunities for consolidation...



# Number and Algebra

Dicey Operations  
American Billions  
Keep it Simple  
Arithmagons  
Pair Products  
Temperature  
Painted Cube

Factors and Multiples Puzzle  
Factors and Multiples Game  
What Numbers Can We Make?  
Peaches Today, Peaches Tomorrow...  
What's Possible?  
Attractive Tablecloths  
How Old Am I?



# Geometry and Measures

Isosceles Triangles

Can They Be  
Equal?

Translating Lines

Opposite Vertices

Coordinate  
Patterns

Route to Infinity

Pick's Theorem

Cuboid Challenge

Semi-regular Tessellations

Warmsnug Double Glazing



# Handling Data

M, M and M

Which List is Which?

Odds and Evens

Which Spinners?



# Interactive tasks

[GOT IT](#)

[Dozens](#)

[Mixing Lemonade](#)

[Missing Multipliers](#)

[Shifting Times Tables](#)

[Finding Factors](#)

[Charlie's Delightful Machine](#)

[Factors and Multiples Game](#)

[Connect Three](#)

[Estimating Angles](#)

[Square It](#)

[Treasure Hunt](#)

[Diamond Collector](#)



...and for even more, see the  
Curriculum Mapping  
Document



# Using rich tasks to introduce new topics



# Start with a rich challenge

To:

Introduce new ideas

Develop understanding of new curriculum content

Discover important mathematical results



# Fruity Totals



# What's it Worth?

Each symbol has a numerical value.

The total for the symbols is written at the end of each row and column.

Can you find the missing total that should go where the question mark has been put?

▲	■	■	▲	28
◆	■	◆	■	30
●	▲	●	●	18
●	■	●	●	20
?	30	23	22	



# Right Angles

Join any two points on the edge to the middle to form a triangle.

Can you work out the angles in your triangle?

Can you join three points on the edge to form a right-angled triangle?



# Mathematics is not a spectator sport

Exploring

→ Noticing Patterns

→ Conjecturing

→ Generalising

→ Explaining

→ Justifying

→ Proving



# The role of the teacher

## Teacher's role

- To choose tasks that allow students to explore new mathematics
- To give students the time and space for that exploration
- To bring students together to share ideas and understanding, and draw together key mathematical insights



There are many more NRICH tasks that make excellent starting points...



# Number and Algebra

Summing Consecutive Numbers

Number Pyramids

What's Possible?

What's It Worth?

Perimeter Expressions

Seven Squares

Attractive Tablecloths



# Geometry

Painted Cube

Cyclic Quadrilaterals

Semi-regular Tessellations

Tilted Squares

Vector Journeys



# Handling Data

Statistical Shorts

Odds and Evens

Which Spinners?



... a teacher of mathematics has a great opportunity. If he fills his allotted time with drilling his students in routine operations he kills their interest, hampers their intellectual development, and misuses his opportunity. But if he challenges the curiosity of his students by setting them problems proportionate to their knowledge, and helps them to solve their problems with stimulating questions, he may give them a taste for, and some means of, independent thinking.

*Polya, G. (1945) How to Solve it*



I don't expect, and I don't want, all children to find mathematics an engrossing study, or one that they want to devote themselves to either in school or in their lives. Only a few will find mathematics seductive enough to sustain a long term engagement. But I would hope that all children could experience at a few moments in their careers ... the power and excitement of mathematics ... so that at the end of their formal education they at least know what it is like and whether it is an activity that has a place in their future. *David Wheeler*



# Keep in touch

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