## Age 14+ Level $\star$ Worksheet 1 - Solutions

1. Average Discovery

The fifth number is 9
nrich.maths.org/5691/solution
2. Partial Means

The mean of the last 28 numbers is 100 nrich.maths.org/6718/solution
3. Mean Balance
$P=9$
$\square=6$
nrich.maths.org/12810/solution
4. Beta Rovers

The mode is 1 goal per match The median is 2 goals per match nrich.maths.org/14354/solution
5. Ladybird Football Team

The pine ladybird has 4 spots nrich.maths.org/11671/solution

These problems are adapted from UKMT (ukmt.org.uk) and WMC (competition.ac) problems.

## Age 14+ Level $\star \star$ Worksheet 1 - Solutions

## 1. Smallest Range

The smallest possible range is 4
(when the integers are 2015, 2016, 2018, 2019)
nrich.maths.org/13522/solution
2. Equal Means
$x=19$
nrich.maths.org/11697/solution
3. Dopey Measurement

The mean height of the Seven Dwarfs is 112.8 cm (to 1 d.p.) nrich.maths.org/6252/solution
4. Driving Test

Mallick has the highest pass rate nrich.maths.org/14007/solution

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## Age 14+ Level $\star \star$ Worksheet 2 - Solutions

## 1. Gamma City

The mode is 0 goals per match
The median is 1 goal per match
nrich.maths.org/14355/solution
2. Mean Median

The median weight of the children is 48 kg nrich.maths.org/12618/solution
3. Acceptance Rate

The school accepted 390 students in 2011
nrich.maths.org/12588/solution

## 4. A Mean Calculation

One possible approach:
Subtracting 100 from each of the numbers gives
$\begin{array}{llllllllllllll}-3 & -3 & -2 & -1 & -1 & -1 & 0 & 0 & 1 & 1 & 3 & 4 & 4 & 5\end{array}$
These numbers add up to 7 , so their mean is $7 \div 14=0.5$
So the mean of the original numbers is 100.5. nrich.maths.org/12851/solution

These problems are adapted from UKMT (ukmt.org.uk) and WMC (competition.ac) problems.

## Age 14+ Level $\star \star$ <br> Worksheet 3 - Solutions

## 1. Algebraic Average

The mean of $y$ and $z$ is $x$
nrich.maths.org/5756/solution
2. Maximum Mean

The largest possible value for the mean is 54 nrich.maths.org/13795/solution
3. Sample

Opportunity samples:
The first came from the second population the second came from the third population the third came from the first population

## Systematic samples:

The first came from the third population the second came from the second population the third came from the first population

The random samples could have come from any of the population samples, but it is likely that the samples with more blue squares came from the populations with more blue squares
nrich.maths.org/14097/solution

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## Age 14+ Level $\star \star \star$ Worksheet 1 - Solutions

## 1. Jewellery Boxes

The total value of the jewels is $£ 24000$ nrich.maths.org/3104/solution
2. Possible Range

The largest possible range is 7 nrich.maths.org/12625/solution
3. Very Average
$a=200$
nrich.maths.org/14223/solution
4. Changing Averages
$m=20$
nrich.maths.org/13668/solution

## 5. Pay Attention

On average 58\% of the talk was heard nrich.maths.org/12867/solution

These problems are adapted from UKMT (ukmt.org.uk) and WMC (competition.ac) problems.

