## Age 14+ Level $\star$ Worksheet 1

## 1. Flipping Coins

A fair coin is flipped 4 times.
What is the probability of getting heads at least 3 times?
2. Boy or Girl

A witch claims that she can predict whether your baby will be a boy or girl, and she charges $£ 100$ for this service.
If her prediction is wrong, she offers to return your $£ 100$ fee and pay you an extra $£ 50$ compensation for any distress that she may have caused.

Assuming she does not have any supernatural powers, can you explain whether she is likely to make a profit or loss after 100 clients have given birth?

## 3. Collecting Marbles

A bag contains hundreds of red, orange, green and blue marbles. Marbles are drawn randomly from the bag, one at a time, and not replaced.

How many marbles must be taken out of the bag in order to ensure that at least three are of the same colour?
4. Tying the Rope

Sam is holding two lengths of rope by their mid-points.
Pat chooses two of the loose ends at random and ties them together.
What is the probability that both pieces of rope are tied together?

## 5. Swapping Sweets

Kate and Anna each have a bag that contains a red sweet, a blue sweet, a green sweet and a yellow sweet.

Without looking, Kate takes a sweet out of her bag and puts it into Anna's bag. Then, without looking, Anna takes a sweet from her bag and puts it into Kate's bag.

What is the probability that after this, each bag contains a red sweet, a blue sweet, a green sweet and a yellow sweet?

These problems are adapted from UKMT (ukmt.org.uk) and WMC (competition.ac) problems.

