## Age 14+ Level $\star \star$ Worksheet 4

1. Sum $=$ Product $=$ Quotient

How many pairs of numbers $(a, b)$ exist such that the sum $a+b$, the product $a b$, and the quotient $\frac{a}{b}$ are all equal?
2. Near 10

How many integers $n$ exist such that the difference between $\sqrt{n}$ and 10 is less than 1 ?
3. Weighing Scales

Two pyramids and a sphere on one side of a pair of scales will just balance a cube on the other side.


A sphere and a cube together will just balance three pyramids.

4. Day of the Triffids

Jasmine spends exactly $£ 120$ on three types of plants.
Poison ivy plants cost $£ 2$ each.
Deadly nightshade plants cost $£ 9$ each.
Triffid plants cost $£ 12$ each.

She buys twenty plants in total, including at least one of each type. How many triffids did she buy?

## 5. Algebraic Differences

If $6 x-y=21$ and $6 y-x=14$, what is the value of $x-y$ ?

## 6. Oldest and Youngest

Edith had nine children at regular intervals of 15 months.
If the oldest is now six times as old as the youngest, how old is the youngest child?

These problems are adapted from UKMT (ukmt.org.uk) and WMC (competition.ac) problems.

