## Age 11+ Level $\star$ Worksheet 1 - Solutions

## 1. No Matter

My answer will always be a multiple of 7
nrich.maths.org/2532/solution
2. Nine in a Line

The largest number is 227
nrich.maths.org/5752/solution
3. Adding and Multiplying

The answer would have been 3165
nrich.maths.org/12817/solution
4. Cube Pile

A tower of all five cubes would be 50 cm tall nrich.maths.org/11712/solution
5. 8 in a Row

The largest is 11
nrich.maths.org/12613/solution
6. Paul's Children

His sons' ages add up to 12
nrich.maths.org/11639/solution

These problems are adapted from UKMT (ukmt.org.uk) and SEAMC (seamc.asia) problems.

## Age 11+ Level $\star \star$ <br> Worksheet 1 - Solutions

## 1. Standing on the Table

The table is 90 cm tall nrich.maths.org/11717/solution

## 2. Square Total

The smallest positive integer is 5
nrich.maths.org/11703/solution
3. Adding in Pairs

The numbers are 18,21 and 30 , so the largest is 30 nrich.maths.org/13384/solution

## 4. Multiple Magic

Your answer will always be a multiple of 3
nrich.maths.org/6260/solution
5. Building Up
$x=360$
nrich.maths.org/10164/solution

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## Age 14+ Level $\star \star$ Worksheet 1 - Solutions

1. Divisible Expression
$(1+x+y)^{2}-(1-x-y)^{2}=4 x+4 y=4(x+y)$
which is divisible by 4
nrich.maths.org/6738/solution
2. Little Difference
$(x-1)(x+1)-x^{2}=x^{2}-1-x^{2}=-1$
so $2015 \times 2017-2016^{2}=-1$
and $2016 \times 2018-2017^{2}=-1$
nrich.maths.org/10126/solution

## 3. Brian's Number

The largest integer he could have chosen is 21
nrich.maths.org/12570/solution

## 4. Adding to $\mathbf{4 0 0}$

The four integers are 192,96, 64 and 48
nrich.maths.org/11678/solution
5. Order the Products

In order of size, from smallest to largest: $186 \times 214 \quad 210 \times 190 \quad 195 \times 205 \quad 198 \times 202 \quad 200 \times 200$
nrich.maths.org/13573/solution

## 6. Square and Cube

The number is
nrich.maths.org/10120/solution

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Age 14+ Level $\star \star$<br>Worksheet 2 - Solutions

## 1. Cuboid Perimeters

The volume of the cuboid is $35 \mathrm{~cm}^{3}$
nrich.maths.org/12780/solution

## 2. Relative Powers

The number is -3
nrich.maths.org/5017/solution
3. Clever Calculation
$x^{2}-(x-2)(x+2)=x^{2}-x^{2}+4=4$
so $2017^{2}-2015 \times 2019=4$
nrich.maths.org/13223/solution

## 4. Big Fibonacci

The maximum possible value of the first term is 999
nrich.maths.org/9395/solution

## 5. Granny's Age

Our ages add up to 100
nrich.maths.org/10158/solution

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Age 14+ Level $\star \star \star$<br>Worksheet 1 - Solutions

## 1. Choir Boys

The choir has 99 members this year nrich.maths.org/12604/solution

## 2. Stolen Pension

The pensioner had $£ 2057$ before the theft
nrich.maths.org/13219/solution

## 3. Find the Factor

The smaller factor is 63
nrich.maths.org/13753/solution
4. Third Side

The three possible Pythagorean triples are:
7, 24, 25
21, 20, 29
35, 12, 37
so the three possible lengths for the third side are 7, 21 and 35
nrich.maths.org/12809/solution
5. Months and Years

Mary was 12 years old on her last birthday
nrich.maths.org/8678/solution

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