If I gave you a list of decimals, you might find it quite straightforward to put them in order of size. But what about ordering fractions?

A man called John Farey investigated sequences of fractions in order of size - they are called Farey Sequences.

The third Farey Sequence, $F_{3}$, looks like this:

$$
\begin{array}{ccccc}
\frac{0}{1} & \frac{1}{3} & \frac{1}{2} & \frac{2}{3} & \frac{1}{1}
\end{array}
$$

It lists in order all the fractions between 0 and 1 , in their simplest forms, with denominators up to and including 3.

Here is $F_{4}$ :

$$
\begin{array}{llllll}
\frac{0}{1} & \frac{1}{4} & \frac{1}{3} & \frac{1}{2} & \frac{2}{3} & \frac{3}{4}
\end{array} \frac{1}{1}
$$

Write down F5.

## Which extra fractions are in $F_{5}$ which weren't in $F_{4}$ ?

Which extra fractions will be in $F_{6}$ that weren't in $F_{5}$ ?
Where will they appear in the sequence?

There are lots of questions you could explore about Farey Sequences. Here are just a few that we thought of:

- How many extra fractions are there in $F_{11}$ that aren't in $F_{10}$ ?
- How many extra fractions are there in $F_{12}$ that aren't in $F_{11}$ ?
- Is every Farey Sequence longer than the one before? How do you know?
- Is there a way of working out how many fractions there will be in the next sequence?
- So far, all the Farey Sequences except $F_{1}$ have contained an odd number of fractions. Can you find a Farey Sequence with an even number of fractions?

