## Cut out the pieces and rearrange into a coherent proof.

| If I have three consecutive numbers, one of them must be a multiple of 3 . | $(p-1)(p+1)$ is a multiple of both 8 and 3 , so $(p-1)(p+1)$ is a multiple of 24 . |
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|  | $p$ is an odd number, so $p-1$ and $p+1$ must both be multiples of 2 . |
| $(p-1)(p+1)$ is the product of a multiple of 2 and a multiple of 4 , so must be a multiple of 8 . | ( $p-1$ ) and ( $p+1$ ) are consecutive even numbers so either ( $p-1$ ) or ( $p+1$ ) must be a multiple of 4. |
| ( $p-1$ ), $p$, and ( $p+1$ ) are consecutive numbers. | Let $p$ be a prime number greater than 3. |
| $p$ is prime and greater than 3 so cannot be a multiple of 3. | Either ( $p-1$ ) or $(p+1)$ must be a multiple of 3 , so the product $(p-1)(p+1)$ must also be a multiple of 3 . |
| The expression $p^{2}-1$ can be factorised as $(p-1)(p+1)$ | Therefore for any prime number $p$ greater than 3 , $\mathrm{p}^{2}-1$ is a multiple of 24 . |

