

Picturing squares part 2

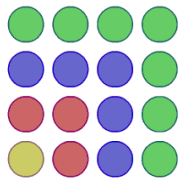
Solutions ;

- How was it built from the original square array?

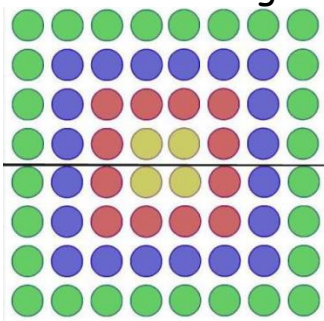
Solution :

So basically to find this out let us first divide the square into 2 .

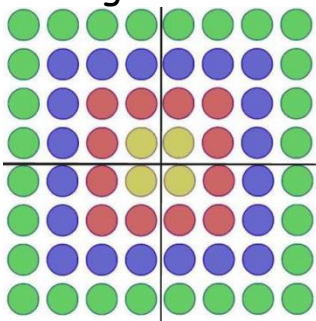
The original square ;



The image when it is divided in 2 ;



We can so far see no relation with the original square . now let us try cutting this in half again :

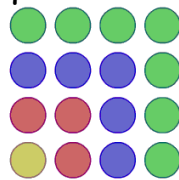


Observation :

- If you observe closely we can see that the quarters are the same size and the same number of colors and dots as the original square except one original picture and 3 other flipped versions of it .
- How many dots there would be in the hundredth diagram (i.e the one with 100 colors)

Solution :

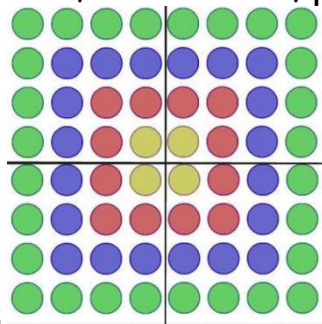
We can see as in the first question that picture one is divided into 4 of the original squares . We can also say this by the number



of dots in each layer .

E.g :

Yellow dots= 1, red dot = 3, purple/blue dots=5, green dots =7



Picture 1 :

Yellow dots=4 , red dots = 12 , purple/blue dots =20 , green dots = 28

As we can see the number of dots in every row increases by x4.
So now we can generalize as the following :

Number of terms(n) x number of terms (n) x4 = number of dots
or

Number of terms (square) x4 = number of dots

E.g : 5 layers/colors

$$5 \times 5 \times 4 = 25 \times 4 = 100 \text{ . or : } 4(5 \text{ square}) = 100$$

100 layer/colors =

$$100 \times 100 \times 4 = 40,000 \text{ . or : } 4(100 \text{ square})$$

The number of dots in 100 layers/colors is 40,000.

- What summation it represents ?

Solution :

It represents summation of :

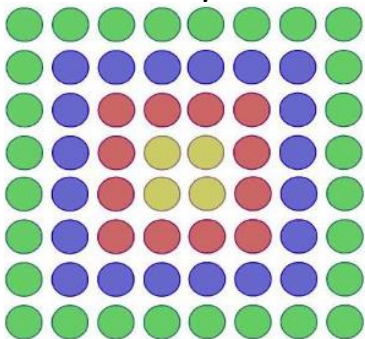
2

$$N \times 4 = \text{summation/number of layer or colors}$$

- Whether there are alternative ways of expressing the summation , relating to different ways of looking at the diagram .

Solution :

Another way of looking at is the sum of the layers :



So the yellow dots = 4 which is 2 square

Then the red dots + yellow dots = 16 = 4 square

Then the red yellow+blue/purple dots = 36 = 6 square

The pattern here you can see is that the square is increasing .

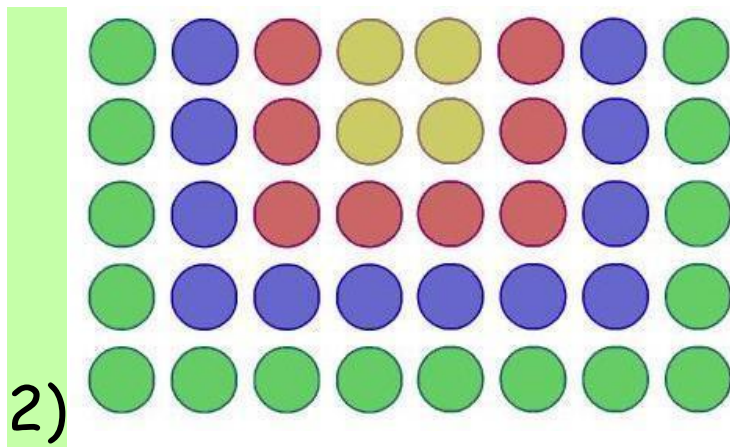
(e.g: 2 square 4 square , 6 square ... etc).

But the way to find it out is ; number of terms x2 then square it

E.g ; (6 layers)

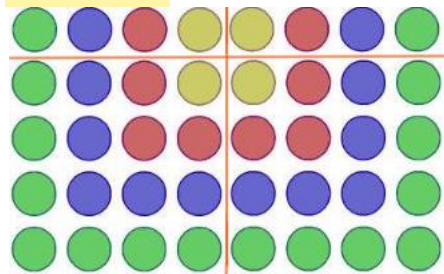
$$6 \times 2 = 12 \text{ , } 12 \text{ square} = 144 \text{ . the number of dots in 6 layers/colors} = 144 \text{ .}$$

So alternative summation = n (no. of terms) $\times 2$ then square it .



- How was it built from the original square array ?

Solution :



Solution :

We can basically see from the above image that there are 2 of the original square arrays and 8 other dots . so we can also see that the above dots are just twice the number of layers/colors . so we can generalize as the following ;

$$2 \times \text{no. of terms} + \text{no. of terms} \times 2 .$$

Example :(2 terms)

$$2 \times 2 + 2 \times 2 =$$

$8+4=12$ and this is right as the number of yellow dots = 4.

Number of

red dots=8. .

- How many dots there would be in the hundredth diagram (i.e the one with 100 colors)

Solution :

$$2 \times \text{no. of terms} + \text{no. of terms} \times 2 .$$

As above this is our formula also explained in the question above . so plug in the numbers and :

$$\begin{aligned} 2 \times 100 + 100 \times 2 &= \\ 2 \times 10,000 + 200 &= \\ 20,000 + 200 &= 20,200 \end{aligned}$$

The number of dots in the hundredth diagram would be 20,200.

- What summation it represents ?

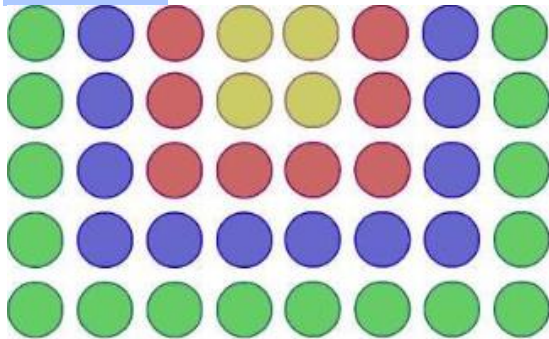
Solution :

$$2 \times \text{no. of terms} + \text{no. of terms} \times 2 .$$

The above is the summation it represents .

- Whether there are alternative ways of expressing the summation, relating to different ways of looking at the diagram.

Solution :



So let us count its colors .

Yellow = 4

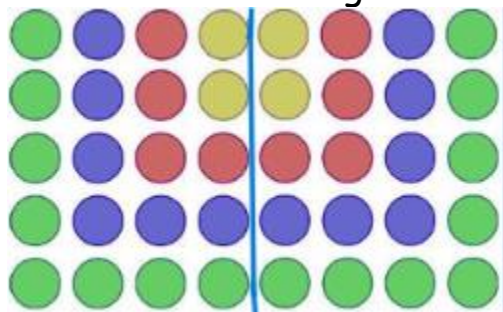
Red = 8

blue/purple=12

green=16

Now we can see that these are just the multiples of 4 .

Let us divide this figure in half and look at it more closely .



We can now see that on each side the colours are now :

yellow=2

red=4

blue/purple=6

green=8

Now if you can observe these numbers connect to the previous homework where we had a similar question . This is also used in the further questions in this document . (fig.3 , fig.4)

So we can use the formula:

No. of terms x number of terms - 1 .

But it doesn't stop here as there is 2 copies of each :

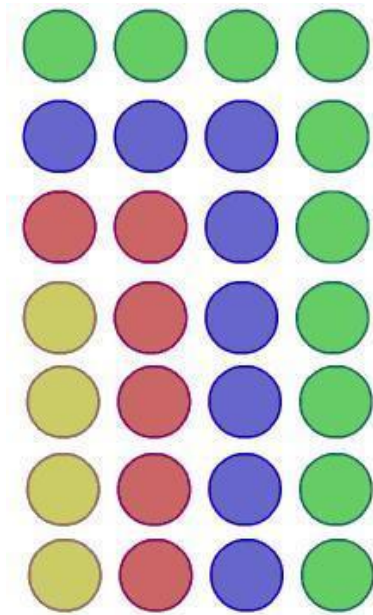
Formula (general):

No. of terms x no. of terms - 1 x 2 =

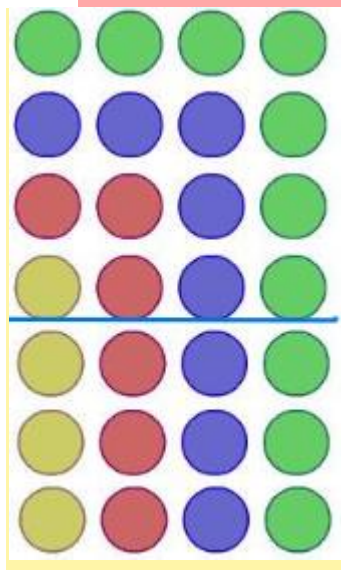
(e.g: 5 layers)

$5 \times 5 - 1(4) \times 2 =$

$5 \times 4 \times 2 = 40 .$



- How was it built from the original square array ?



We can observe we have one copy of the original square + $3 \times 4 = 12$.

So $16+12=28$. Now another thing we can observe here is that the bottom 3×4 , is just multiplying $3 \times$ the number of terms/colors/layers .

So we can generalize as the following :

$$\begin{matrix} 2 \\ \text{No. of terms} + 3 \times \text{no. of terms} . \end{matrix}$$

E.g :(5 colors/layers)

$$\begin{matrix} 2 \\ 5 + 3 \times 5 \\ 25 + 15 = 40. \end{matrix}$$

- How many dots there would be in the hundredth diagram (i.e the one with 100 colors)

Solution:

Lets plug in formula :

$$\begin{matrix} 2 \\ \text{No. of terms} + 3 \times \text{no. of terms} . \end{matrix}$$

Now let us apply this to hundred :

$$\begin{matrix} 2 \\ 100 + 3 \times 100 = \\ 10,000 + 300 = 10,300 \end{matrix}$$

The number of dots that will be there in the hundredth diagram would be 10,300

- What summation it represents ?

Solution :

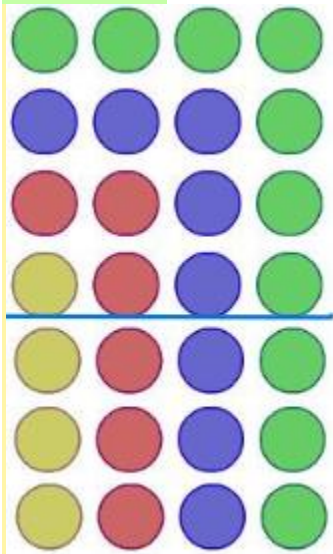
2

No. of terms + 3x no. of terms .

The above is the summation . This is explained in the q.1 for this diagram .

- Whether there are alternative ways of expressing the summation , relating to different ways of looking at the diagram .

Solution :



First let us count its colors :

yellow=4

red=6

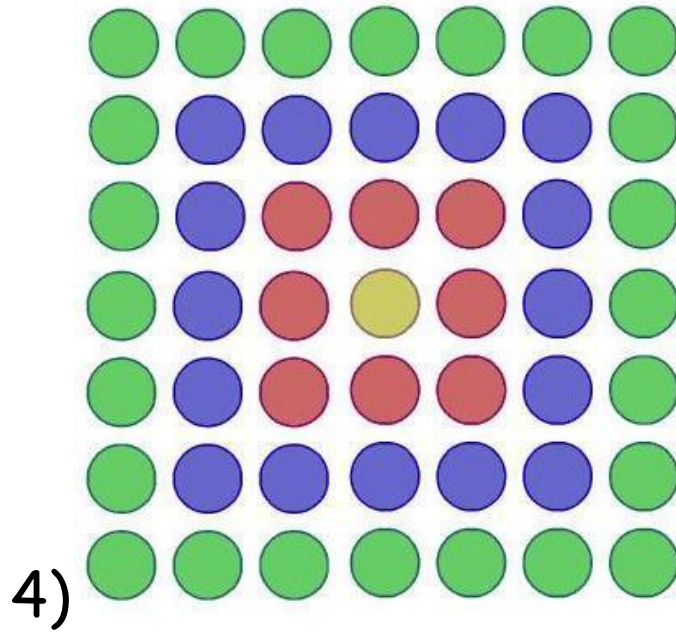
blu/purple=8

green=10

Now we can see this is similar to the question(2+4+6...) as it has gap of two and is missing a 2 so we generalize this as :(in other questions as well fig.2,fig.4)

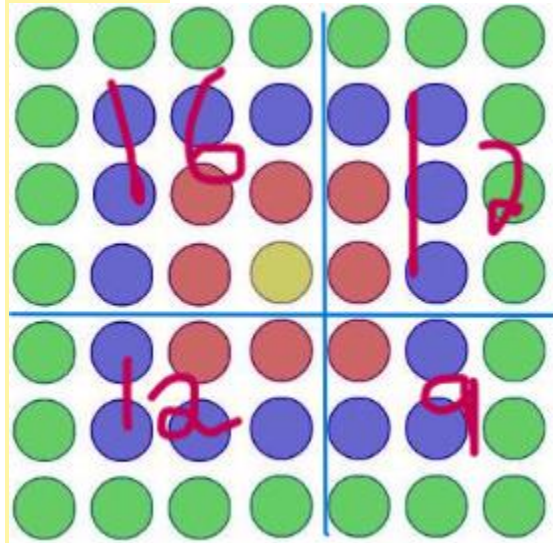
Formula :

No. of terms \times no. of terms - 1.



- How was it built from the original square array ?

Solution :



As we can see there is one copy of the original square diagram and 2 (2+4+6 ...) diagrams which connects to the previous homework as we had the question (2+4+6 ...) , then we have a figure of 3 square (9) .

And we can see the number of terms is 4 , so we square that to get 16,

2

then we use the formula : no of terms

Now we can see there are 2 copies of (2+4+6) .

looking at the picture each of these diagrams are the :

number of terms x number of terms -1

Since there is 2 of this we just multiply it by 2 which is now :

Number of term x number of terms - 1 x2

Let us go further . now we can see that the 3 square (9) now we

can

just

See that is like 4 square but with the base no. 1 less . then we square it .

So we can conclude this :

2

Number of terms -1 .

Put this all together to form the general formula :

2

2

Number of terms + number of terms - 1 + number of terms x numbers of terms - 1 x 2 .

For example : 5 layers

2

2

$5^2 + 5 \times 5 - 1 + (4) \times 2 + 5 - 1(4) =$

$25 + 40 + 16 =$

81

(i have another a less complicated method in the last question of this problem)

- How many dots there would be in the hundredth diagram (i.e the one with 100 colors)

Lets plug in formula :

2

2

Number of terms + number of terms - 1 + number of terms x numbers of terms - 1 x 2 .

2 2

$100 + 100 - 1 + 100 \times 99 \times 2 =$

$10,000 + 9801 + 9900 \times 2 = 10,000 + 9801 + 19800 = 39,601$

The final solution is that in the hundredth figure there will be 39,601 dots

- What summation it represents ?

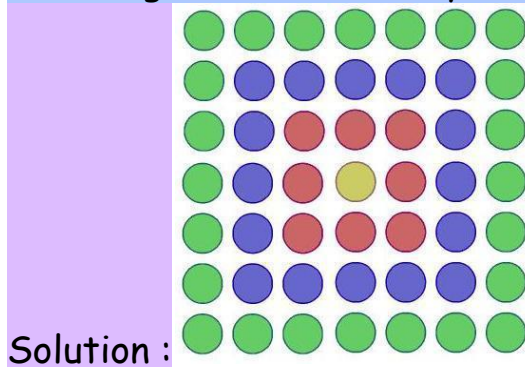
Solution :

2 2

Number of terms + number of terms - 1 + number of terms x numbers of terms - 1 x 2 .

This is what we used in the previous questions. More is mentioned in the following question .

- Whether there are alternative ways of expressing the summation , relating to different ways of looking at the diagram .



Let us observe the number of dots in each color .

yellow=1, red=8, blue/purple=16, green=24

So let us add $1+8=9$. So we can see that 9 is 3 squares , and the number of terms is 2 so we add 1 to the base and square it (for this example),but this doesn't work for every example (e.g $1+8+16 =25$ (5square) this will not work if you add one to 3 (the number of terms) $3+1= 4$ then square it 4 square but the sum of 5 square so this doesn't work .) so another way : $2-1=1$ and we are adding one to base then

squaring it , this can apply to other numbers of layers as well . let us generalize this as :

$$\text{No. of terms} + \text{number terms} - 1$$

e.g :(5 layers or terms)

$$5 + 5 - 1 = 9 = 3^2$$

