



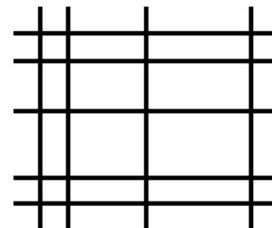
Creating and Manipulating Expressions

Stage 3 ★★

Mixed Selection 1

1. How many rectangles?

By drawing 9 lines, 5 horizontal and 4 vertical, one can form 12 small rectangles, as shown on the right.



What is the greatest possible number of small rectangles that one can form by drawing 15 lines, either horizontal or vertical?

2. Standing on the Table

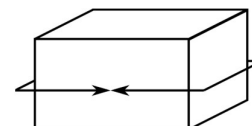
When Clement stands on a table and Dmitri stands on the floor, Clement is 80cm taller than Dmitri. When Dmitri stands on the table and Clement stands on the floor, Dmitri is 1m taller than Clement. How tall is the table?

3. Brothers and sisters

A boy has the same number of sisters as brothers. Each of his sisters has only half as many sisters as brothers. How many brothers and sisters are in the family altogether?

4. Cuboid perimeters

The 'perimeter' of a cuboid can be measured along three axes. One 'perimeter' of this cuboid is shown.



If the perimeters of a cuboid are 12 cm, 16 cm and 24 cm, what is the volume of the cuboid?

5. Square total

Anastasia thinks of a positive integer.
Barry doubles Anastasia's number.
Connor trebles Barry's number.
Damion multiplies Connor's number by 6.

Eve notices that the total of the four numbers is a perfect square. What is the smallest positive integer that Anastasia could have thought of?

These problems are adapted from UKMT (ukmt.org.uk) and SEAMC (seamc.asia) problems.