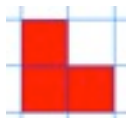


L-triominos

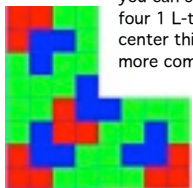


A trimino is a shape made from three squares.
Here is an L-trimino

Can you work out how to use the tiling of a size 2 L-trimino to help you to tile a size 4 L-trimino?

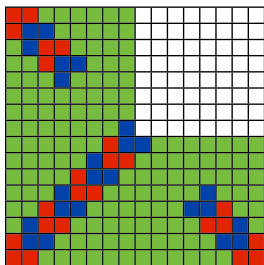
We can do this by realizing we can create any number of L-trimino by placing a 1 L-trimino triangle in the middle and working out the rest, as show in this diagram on the right. By using this method we can build the 4 L-trimino with ease.

we can also see a pattern occurring by highlighting the L-triominos as you can see the 4 L-trimino has four 1 L-trimino running down its center this is the key to build other more complex L-triominos.



4 boxes

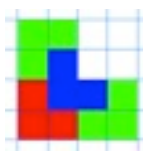
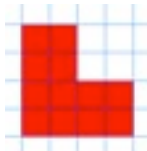
8 boxes



Isaac Blackbourne

16 boxes

Here is a size 2 L-trimino



Devise a convincing argument that you will be able to tile a size 8, 16, 32... $2n$ L-trimino using size 1 L-triominos.

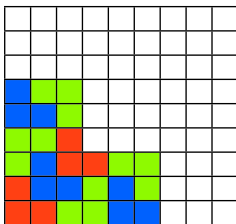
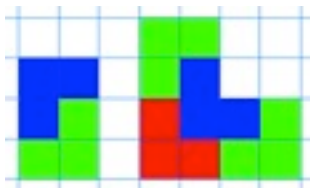
By using the method we used for the 4 L-trimino we can make another larger one for instance an 8 L-trimino as shown on the left. This can be used for any number, the priceable is the same along with the horizontal length being double the number of the L-trimino and the vertical being the same. For instance if it was a 8 L-trimino the horizontal length would be 16 and the vertical would be 8.

How many size 1 L-triominos would you need to tile a size 8... 16... 32... $2n$ L-trimino?

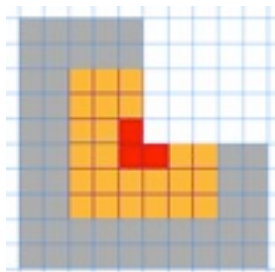
2 L-trimino	4
4 L-trimino	16
8 L-trimino	64
16 L-trimino	256
32 L-trimino	1024

L-triominos

What about odd sized L-triominos? Can you turn a size 1 L-trimino into a size 3 L-trimino using combinations of the 'building blocks' below?



In the same way, can you find a way of adding to your size 3 tiling to tile a size 5? Then a size 7, 9, 11...?



This can be easily done by simply building on what you have at the start. For instance you start with a 1 L-trimino at the start and build to that a 3 L-trimino and so on to what ever number of L-trimino you want.

By using both of these methods for the even and odd number L-triominos it is possible to build any number of L-triominos as the methods are the same for every number of L-triominos and it's just a case of drawing the bases like the corners and the center piece.